

FIG. 4. Dispersion curves of the cross section for photoionization of the ground state of a hydrogen atom by a field of intensity $F_0 = 10^{-2}$ with three different degrees of ellipticity ϵ . Curves 1, 2, 3 correspond to values $\epsilon = 0, 0.5$, and 1.

persion curves are given for the polarizability of the ground state by the field of a linearly polarized wave. Figure 4 shows the dependence of the ionization cross section on the frequency for three different values of the ellipticity of the polarization. The complicated character of the curves reflects the interference of the contributions of the s and d states in Eq. (9). For the shift the main contribution in Eq. (9) is from the term proportional to F_0^2 and independent of the parameter ϵ . Therefore the dependence of the shift of the ground state on the degree of ellipticity is extremely weak.

The approximation made in Sec. 3 corresponds to including only the "field" mechanism of broadening of a

quasistationary level, in which the width is linear in the field strength and is proportional to the matrix element of the resonance transition. The calculations indicate that in fields $F_0 = 3 \cdot 10^{-2}$ this width is of the same order of magnitude as the maximum detuning of the resonance. Summarizing all of these statements, we can say that inclusion of only the field broadening is sufficient, and that in strong fields it is absolutely necessary to include it for a correct description of the interaction of a hydrogen atom with a monochromatic wave.

In conclusion the writers express their gratitude to A. G. Fainshtein for a helpful discussion.

¹An atomic system of units is used in this paper.

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Investigation of transition x-radiation in tin foils

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The transition x-radiation of electrons of energy 1-1.35 GeV was investigated in a tin-foil radiator consisting of $N = 20$ plates each $a = 20 \mu\text{m}$ thick and separated by a distance $b = 1 \text{ mm}$. The experimental spectra are compared with the theoretically calculated ones. The experimental results are in better agreement with the transition x-ray theory that takes into account the influence of multiple scattering.

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Transition radiation in the x-ray band (XTR) has by now been sufficiently well investigated both experimentally and theoretically.¹⁻³ Agreement between the experimental results and the XTR theory is observed in practically all the studies. Only in a few cases is a deviation from the theory observed and ascribed to the influence of multiple scattering.⁴⁻⁶ The characteristics of the deviations observed in Refs. 4 and 5 were ana-

lyzed in Refs. 7-9. The results of Ref. 6, however, have not been explained to this day. Theoretical calculations by Garibyan's group¹⁰ have shown that the experimental results of Ref. 6 cannot be attributed to the influence of multiple scattering.

An investigation¹¹ of XTR in a radiator of copper foils has shown that the XTR theory without allowance for

multiple scattering also describes the experimental result satisfactorily in this case.

A theory of XTR with allowance for multiple scattering has by now been developed for both an isolated plate^{12,13} and a stack of plates.^{14,15} It has therefore become possible to analyze more correctly the experimental results in those cases when multiple scattering can influence the XTR. In particular, it follows from these theoretical papers that for a stack of N absorbing plates of thickness a and with vacuum gaps b , subject to satisfaction of the condition $b \gg Z_{\text{vac}}$, where Z_{vac} is the zone of formation of the transition radiation in vacuum, the frequency distribution of the intensity of the total radiation emerging from the stack, just as in the case where no allowance is made for multiple scattering, is equivalent to emission from a single plate, multiplied by the effective number of plates N_{eff} , where

$$N_{\text{eff}} = (1 - e^{-N\mu}) / (1 - e^{-\mu}) \quad (1)$$

(μ is the linear absorption coefficient in the medium).

Yan Shi¹⁵ has shown, in particular, that the total radiation from an absorbing plate can be divided into two parts: 1) a part due to the presence of boundaries (edge effect in the total radiation) and 2) a part corresponding to bremsstrahlung from a path length equal to the effective thickness of the plate, in other words,

$$\left\langle \frac{dW(\omega)}{d\omega} \right\rangle_{1,a}^{\text{tot}} = \left\langle \frac{dW(\omega)}{d\omega} \right\rangle_{1,a}^{\text{cr. eff}} + \frac{a_{\text{eff}}}{Z_{\text{br}}} \frac{dW_M(\omega)}{d\omega},$$

where $Z_{\text{br}}^{-1} dW_M(\omega)/d\omega$ is the bremsstrahlung emitted from a unit length in an unbounded medium, Z_{br} is the zone of bremsstrahlung formation, and $a_{\text{eff}} = (1 - e^{-\mu a})/\mu$.

In experiment one always measures the total radiation, therefore to determine the expression for $dW(\omega)/dW_{1,a}^{\text{cr. eff}}$ it is necessary to measure $(a_{\text{eff}}/Z_{\text{br}}) dW_M(\omega)/dW$ separately. Usually one measures for this purpose the radiation from a solid radiator with thickness equal to the summary thickness of the layered radiator, but it is clear that in this method of XTR separation no account is taken of the contribution of the two boundaries of the equivalent radiator. In the case of a large number N of plates and small $\mu(\omega)$, the resultant error is small, but for small N and large $\mu(\omega)$ the influence of the boundaries of the equivalent radiator may become substantial.

In this study we used tin as the radiator material. (This is precisely the material where a quadratic dependence of the total number of photons on the electron energy was observed⁶ in contradiction to the theory.) We used a radiator consisting of twenty plates each $a = 20$ m thick and spaced $b = 1$ mm apart.

The measurements were made at electron energies 1–3.5 GeV, using the secondary electron beam of the Erevan accelerator. The experimental setup is described in detail in Ref. 8. In this installation, the dimensions of the apparatus counters were decreased to $20 \times 20 \times 15$ mm. This made it possible to localize more accurately the trajectories of the electrons passing through the radiator and through the entire installation.

The XTR detector was a spectrometric scintillation counter based on an NaI (Tl) crystal. The crystal had a diameter $\Phi = 7$ cm, a thickness 2 cm, and an acceptance angle $\sim 6.5 \times 10^{-3}$. The detector was calibrated against radioactive sources in the gamma-quantum energy range 34–250 keV.

The experimental spectra described below were obtained after taking into account the corrections for the multiplicity of the photons and for the losses due to the characteristic radiation in the NaI(Tl), for the influence of the finite resolution of the spectrometer,^{16,17} and for the absorption of the gamma quanta along the path from the radiator to the spectrometer. To take into account the bremsstrahlung as well as the background in the laboratory, we measured each time the radiation from an equivalent tin-plate radiator 400 μm thick. The contribution of the XTR produced on the two boundaries of the equivalent radiator was determined by theoretical calculation. For the radiator in question, at $E_e \geq 2.0$ GeV, this correction amounts to $\sim 15\%$ in the $\hbar\omega$ region 20–35 keV, and is negligible at $\hbar\omega > 40$ keV.

Since the condition $b \gg Z_{\text{vac}}$ for the independence of the radiation from individual plates are satisfied in our case for practically all the considered frequencies and energies of the electrons, the theoretical calculations were made for an isolated plate and recalculated for a stack by multiplying by N_{eff} . If we disregard the influence of the multiple scattering, then discrimination with respect to the emission angle leads in our case to a decrease in the number of photons by $\sim 45\%$, $\sim 10\%$, $\sim 1\%$ at photon energies $\hbar\omega$ 20–25, 30–35, and > 50 keV respectively, regardless of the electron energy.

Figure 1 shows the XTR spectra calculated with (dashed curves) and without (solid curves) allowance for multiple scattering at an electron energy 1, 2, 3, and 3.5 GeV. The abrupt decrease in the region $\hbar\omega \sim 31$ keV is due to the presence of the K absorption edge. It follows from the figures that under our conditions the influence of multiple scattering leads to a $\sim 25\%$ lowering of the XTR spectra in the region of the right-hand maximum, but in the other frequency regions the change is negligible. The same figure shows the experimental XTR spectra for the same electron energies (points).

It follows from Fig. 1 that at an electron energy $E_e \geq 2$ GeV in the photon energy range $40 \text{ keV} \leq \hbar\omega \leq 100 \text{ keV}$ the experimental results agree better with calculations that take multiple scattering into account. Unfortunately, the energy resolution of the γ spectrometer is insufficient to observe a narrow maximum in the region $\hbar\omega \sim 28$ keV. This, obviously, leads to a smoothing of the maximum and accordingly to an increase in the number of the observed photons in the vicinities of this maximum. Appreciable discrepancies are observed between the experimental results and the theory at $E_e = 1.0$ GeV. This fact can be qualitatively explained in the following manner. As already mentioned, the theoretical spectra were calculated for one plate, and the conversion for a stack of plates was with the aid of expression (1). It is clear that this method takes correct account of the photon absorption, but the additional radiation divergence angle, due to the multiple scattering of the

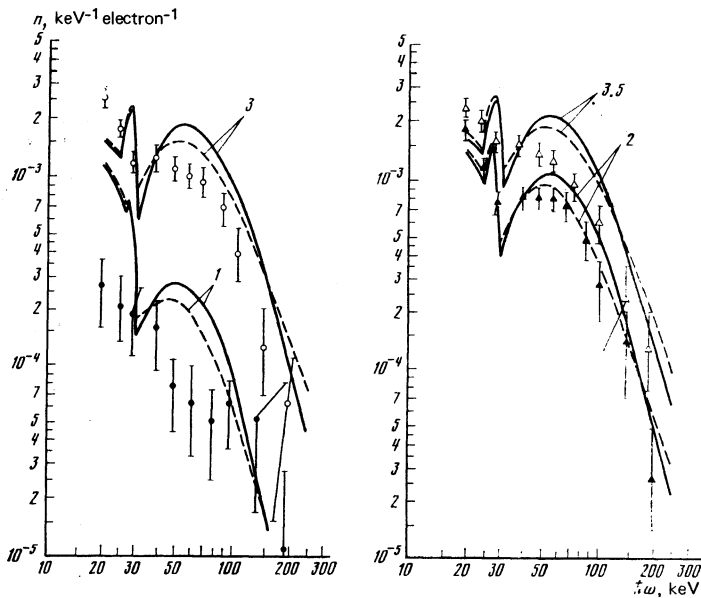


FIG. 1. XTR spectra produced in a stack of tin foils. The numbers on the curves correspond to different values of the electron energy E_e in GeV: ●—1; ▲—2, ○—3, △—3.5.

electrons in the stack, is not accounted for here. Since the multiple-scattering angle is inversely proportional to the particle energy, the photon loss for low electron energies, due to the finite dimensions of the gamma spectrometer, is larger than for high energies.

In addition, it appears that the angle spread of the radiation in the presence of multiple scattering is larger than in its absence. Therefore the finite dimensions of the gamma spectrometer lead in this case, too, to a stronger decrease of the fraction of the photons registered at small E_e than at large E_e . Obviously, this qualitative analysis is insufficient to explain the experimental results, and for a final solution of the problem it is necessary to have theoretical spectra integrated in the region of the angles within which the photons are registered in experiment.

Figure 2 shows the dependence of the average number of XTR photons on electron energy. The solid and

dashed curves show the results of the theoretical calculations without and with allowance for multiple scattering, while the points show the corresponding experimental results. It is seen from the figure that the number of photons increases linearly with increasing energy up to $E_e = 2.5$ GeV, while at $E_e > 2.5$ GeV this dependence becomes weaker, whereas the theoretical dependence remains linear in the entire range of E_e . The experimental points lie somewhat lower in the entire interval than the corresponding theoretical values and agree better with the theory that takes multiple scattering into account.

Figure 3 shows the dependence of the total XTR energy release W on E_e . The solid and dashed curves correspond to theoretical calculations without and with allowance for multiple scattering, while the points show the experimental results. As seen from the figure, a linear dependence of W on E_e is expected here, too. A similar dependence is observed experimentally, but with a smaller slope than in the theory.

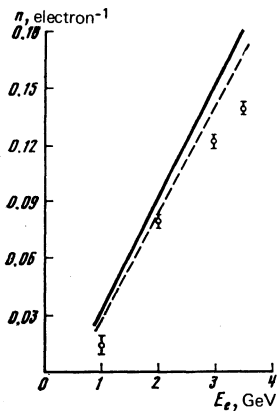


FIG. 2. Dependence of the total number of quanta n on the electron energy.

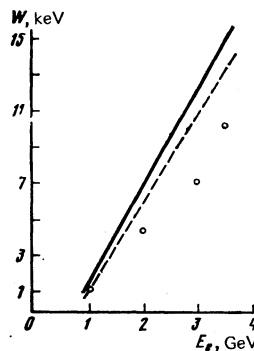


FIG. 3. Dependence of the total radiation energy on the electron energy.

Thus, the results of our investigations show that the quadratic dependence of W on E_0 , observed in Ref. 6 for XTR in tin granules, does not appear in the case of a layered radiator made of the same material. It is possible that this disparity is due to the different methods of generation and registration of the XTR.

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Collapse of 4f-electron in the configuration $3d^9 4f$ in xenonlike ions

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The $M_{4,5}(3d)$ absorption and emission spectra of the xenonlike ions I^- , Cs^+ , Ba^{2+} , and La^{3+} were measured in ionic compounds (spectral range 600-1100 eV). It is shown that the form of the spectrum characterizes mainly the absorbing ion and depends little on its surrounding. The absorption spectra of Cs^+ , Ba^{2+} , and La^{3+} contain an intensive doublet near the ionization threshold of the $3d$ shell, and their emission spectra contain bands that are at resonance with the absorption bands. It is concluded that in the Ba^{2+} and La^{3+} ions the $4f$ orbit in the configuration $3d^9 4f$ is collapsed and that its collapse takes place on going from Xe to Cs^+ . This conclusion is confirmed by a calculation of the energies and cross sections of the $3d^{10} \rightarrow 3d^9 4f$ transitions in the Hartree-Fock-Pauli approximation.

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1. INTRODUCTION

The phenomenon of sudden compression of the radial wave function of an excited electron in a number of neutral atoms or in an isoelectronic sequence, which was named electron collapse, was predicted by Fermi in 1928.¹ Only in the last decade, however, in connection with the extensive studies of excited configurations of atoms and ions, did it attract considerable attention and made it possible to explain a number of interesting effects in atomic spectra and in the physics of atomic collisions.^{2,3}

The effective potential in the centrosymmetric field in the Hartree-Fock equation for the electron nl consists of two terms:

$$V_{\text{eff}}(nl|r) = V(nl|r) + l(l+1)/r^2,$$

where $V(nl|r)$ is the potential of the Coulomb field of the nucleus and of the other electrons, while the second term is centrifugal. In the interval $r \approx 1-5$ a. u., $V(nl|r)$ varies approximately like r^{-2} , and in the case of an electron with $l \geq 2$ these two terms compete with each other in a certain interval of r .² This leads to a specific form of the effective potential, with two minima separated by a positive potential barrier. The localization of the electron in the field of this potential is highly sensitive to a change in the charge of the nucleus or of the states of the other electrons. Whereas in a certain configuration of the atom Z the wave function of the excited electron is localized predominantly in the region of the outer potential well, for the same configuration of