

of error (15 to 20%), these authors also obtained agreement between the form of the spectrum and curve (1).

In our earlier work,<sup>4</sup> estimates were obtained of the temperatures of fragments from  $U^{233}$  and  $Pu^{239}$  relative to  $U^{235}$ , equal to  $(1.04 \pm 0.01)$  and  $(1.05 \pm 0.01)$  Mev. The value of the function  $F(E)$  for parameters  $\omega = 0.5$  Mev,  $T_0 = 1$  Mev,  $T_1 = 1.03$  Mev,  $T_2 = 1.06$  Mev in the spectrum energy region  $0 - 1$  Mev differ from each other by not more than 4%, which is less than the accuracy of our measurements.

In this work, we also determined the ratio of the number of recoil protons in the interval  $0.05 - 0.6$  Mev to their number with energies  $> 0.6$  Mev was also determined. The experimental values of the ratios for  $U^{233}$ ,  $U^{235}$ , and  $Pu^{239}$  are respectively equal to  $0.49 \pm 0.04$ ,  $0.53 \pm 0.04$ , and  $0.48 \pm 0.04$ . A calculation using formula (1) and the parameter values given above gave for these values the numbers 0.5, 0.52, and 0.495.

Thus, the measurements of fission neutron

spectra in the region of low energies are in agreement with the results of Ref. 4, confirming the conclusion that the previously noted difference in the fission neutron spectra of  $U^{233}$ ,  $U^{235}$ , and  $Pu^{239}$  lies in the high energy region.

In conclusion I express my gratitude to I. I. Bondarenko and O. D. Kazachkovski for suggestions and discussion of the results and to A. I. Leipunskii for his continued interest in this work.

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### SYSTEMATICS OF THE AVERAGE NUMBER $\nu$ OF PROMPT FISSION NEUTRONS

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THE number  $\nu$  of prompt neutrons emitted during fission, is determined by the energy balance equation

$$E_f = E_k + E_x = E_k + \nu E_n + E_\gamma, \quad (1)$$

in which  $E_f$  is the fission energy,  $E_k$  and  $E_x$  are the kinetic and the excitation energies of the pair of fragments, and  $\nu E_n$  and  $E_\gamma$  are the energies carried by the prompt neutrons and  $\gamma$  rays respectively. In this work we compare the experimental values of  $\nu$  (Refs. 1-8) with the results of calculations based on the assumptions that will be discussed below.

We considered the masses of only two fragments, a light one  $M_l$  and a heavy one  $M_h$ , corresponding to the most probable method of fission. When calculating the fission energy, the mass of the fissioning nucleus  $M(A, Z)$  was determined from the Green<sup>9</sup> semi-empirical formula, and the masses of the fission fragments  $M(A_l, Z_l)$ ,  $M(A_h, Z_h)$  were calculated by the Fermi formula

with the Fong correction factors,<sup>10</sup> which take into account the shell structure of the nuclei. Since the mass of the heavy fragment varies slightly<sup>11</sup> over the wide range  $232 < A < 252$ , owing to the shell effect, and has an average value  $139 \pm 3$ , we assumed for simplicity  $A_h = 140$  (prior to the neutron emission). The values of  $Z_l$  and  $Z_h$ , the initial charges of the fission fragments, are calculated subject to the hypothesis of equal  $\beta$ -decay chains.

The kinetic energy  $E_k$  of the fission fragments was calculated from the formula

$$E_k = c_1 Z^2 A^{-1/3} (1 - c_2 Z^2 / A), \quad (2)$$

obtained by representing  $E_k$  as the Coulomb repulsion energy of two charged deformed spheres.<sup>10</sup> The constants  $c_1$  and  $c_2$  are chosen to obtain the best fit between Eq. (2) and the experimental values of  $\nu$  in Eq. (1).

The average energy  $E_n$  carried by a prompt neutron consists of the binding energy  $E_b$  of the last neutron in the fragment and its mean kinetic energy  $2T$  with respect to the fragment at rest. The temperature  $T$  of the fragment, after the emission of the neutron, was estimated from data on the neutron spectra of the fission of  $U^{233}$ ,  $U^{235}$ , and  $Pu^{239}$  by thermal neutrons<sup>12</sup> and the spontaneous fission of  $Cf^{252}$  (Ref. 13). The values of  $E_b$  were calculated from the mass formula of Fermi-Fong.<sup>10</sup> The value  $\nu_l/\nu_h = 1.3$ , obtained by Fra-

ser<sup>14</sup> for the fission U<sup>235</sup> by thermal neutrons, was extended to include the entire nucleus under consideration. The calculated values of E<sub>n</sub> were found to be in good agreement with measured values of dν/dE<sub>X</sub> = 1/E<sub>n</sub> (Refs. 15—17).

The mean energy E<sub>γ</sub> of the instantaneous γ rays was assumed constant, 8 Mev, in the calculations, as confirmed by experiments on the study of the prompt-fission γ rays from U<sup>235</sup>(n, f) and Cf<sup>252</sup> (Refs. 15, 18).

For comparison with the calculations, all the experimental values of γ, for the fission induced by neutrons, were reduced to values of ν for spontaneous fission of the corresponding compound nuclei, using the formula dν/dE<sub>X</sub> = 1/E<sub>n</sub>. The validity of this operation was confirmed by direct comparison of ν for the processes Pu<sup>235</sup>(n, f) and Pu<sup>241</sup>(n, f) (Ref. 5) with ν for spontaneous fission of Pu<sup>240</sup> and Pu<sup>242</sup> (Refs. 1—3).

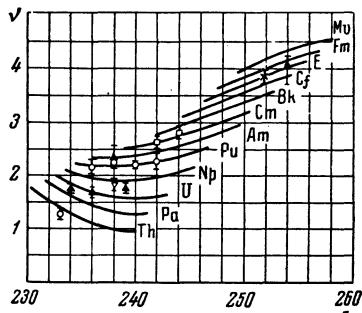


Fig. 1. Dependence of the average number of prompt fission neutrons on A, for various Z. Lower point o—Th, ▲—U, ▽—Np, □—Pu, □—Cn, ×—Cf, ●—Fm.

The diagram shows a family of curves of ν as functions of A for various Z. Most experimental data are in satisfactory agreement with the calculations. An exception is the value of ν for the spontaneous fission of U<sup>238</sup> (Ref. 7). The value of ν for the spontaneous fission of Th<sup>232</sup> was not compared with the results of these calculations, for according to the latest measurements for the period of spontaneous fission of Th<sup>232</sup> (Ref. 19), there is a certain doubt concerning the value ν<sub>Th</sub>/ν<sub>U</sub> = 1.07 ± 0.1 (Ref. 6).

The non-monotonic course of ν(A) is due to the shell structure of the fragments. Without taking the shells into account, dν/dA > 0. On nuclei with A < 240, i.e., with A<sub>f</sub> < 100, the nearness of a shell with 50 neutrons manifests itself—the excitation energy increases with diminishing A, and the sign of dν/dA is reversed.

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#### ON THE DOUBLE BETA-DECAY OF Ca<sup>48</sup>

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A number of experimental researches have shown<sup>1,2</sup> that the period of double β-decay is greater than 10<sup>18</sup> years. In this connection, the necessity has arisen of re-examining the esti-