

quency of 58 mc and acceleration time of 10,000 μ -sec. Preliminary investigation shows the azimuthal spread of the electron bunch at the end of the cycle is $100 \pm 10^\circ$.

A detailed description of the method and results of this experiment will be published at a later date.

The author expresses his sincere gratitude to Prof. P. A. Cerenkov for valuable discussions.

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Translated by C. R. Lubitz
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On the Derivation of a Formula for the Energy Spectrum of Liquid He⁴

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(Submitted to JETP editor June 10, 1956)

J. Exptl. Theoret. Phys. (U.S.S.R.) 31, 536-537

(September, 1956)

As is well known, Feynman¹, using a wave function of a special form, has obtained an expression for the spectrum of the elementary excitations in liquid He⁴. A hydrodynamical derivation of this formula is presented below.

We shall begin with the Hamiltonian for a quantum liquid in the form²

$$\hat{H} = \frac{1}{2} \int \hat{m} \hat{v} n \hat{v} d\tau + \hat{H}^1 [n], \quad (1)$$

where n is the number of atoms per unit volume and $\hat{H}^1 [n]$ is the velocity-independent part of the Hamiltonian. We shall assume it to be a function of n . We set $n = \bar{n} + \delta n$ and expand H in terms of the second order in δn . The first-order term drops out and we obtain

$$\hat{H} = \hat{H}^1 [\bar{n}] + \frac{\bar{m}\bar{n}}{2} \int \hat{v}^2 d\tau + \int \varphi(r, r') \delta n \delta n' d\tau d\tau', \quad (2)$$

where φ is the second functional derivative of \hat{H}^1 with respect to n . Transforming now to Fourier components

$$\delta n = \sum_{\mathbf{k}} n_{\mathbf{k}} e^{i\mathbf{k}\mathbf{r}}$$

and taking into account the equation of continuity in the form

$$\delta \dot{n} + \bar{n} \operatorname{div} \hat{v} = 0, \quad (3)$$

as well as the fact that φ depends only upon $|r - r'|$, we obtain

$$\hat{H} = \hat{H}^1 [\bar{n}] + \sum_{\mathbf{k}} \left(\frac{m |\dot{n}_{\mathbf{k}}|^2}{2\bar{n}k^2} + \frac{1}{2} \varphi_{\mathbf{k}} |n_{\mathbf{k}}|^2 V \right). \quad (4)$$

This expression has the form of a sum of the Hamiltonians of oscillators having frequencies:

$$\omega^2(\mathbf{k}) = (k^2 \varphi_{\mathbf{k}} \bar{n} / m) V. \quad (5)$$

For the determination of $\varphi_{\mathbf{k}}$ we note that the average value of the potential energy of an oscillator in the ground state is equal to $\hbar \omega / 4$, whence

$$\frac{1}{2} \varphi_{\mathbf{k}} \overline{|n_{\mathbf{k}}|^2} V = \frac{1}{4} \hbar \omega(\mathbf{k}). \quad (6)$$

As is well known, however, $S(k) = |\bar{n}_k|^2 / \bar{n}$ is the Fourier component of the correlation function for the atoms of a liquid, which can be determined from diffraction experiments. Substituting $\varphi_{\mathbf{k}}$ from (6) into (5), we find for the energy of excitation

$$E(\mathbf{k}) = \hbar \omega(\mathbf{k}) = \hbar^2 k^2 / 2mS(k),$$

which agrees with Feynman's result.

In conclusion, I would like to express my thanks to L. D. Landau for his advice.

¹ R. P. Feynman, Phys. Rev. 94, 262 (1954).

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Translated by S. D. Elliott
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The Effect of a Transverse Magnetic Field on the Thermal Conductivity of Metals

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(Submitted to JETP editor February 26, 1956)

J. Exptl. Theoret. Phys. (U. S.S.R.) 31, 331

(August, 1956)

LET us consider a metal, in which there is a heat flow $Q = Q_x$ and a magnetic field $H = H_x$. For the calculation of the coefficient of thermal conductivity we use the model of Sommerfeld,¹ according to which the flow depending on the motion of electrons under the action of the temperature gradient is set equal to zero. Accordingly,²

$$I_x = -\frac{3ne}{mv^3} \int \xi f v d\varepsilon, \quad Q_y = \frac{3n}{2v^3} \int \eta f v^3 d\varepsilon \quad (1)$$

and analogously for I_y and Q_x . Here $(-e)$ is the charge on the electron, m is the mass of the electron, v is the velocity, ξ and η are the components of the velocity along the x and y axes, ε is the kinetic energy of the electron. The distribution function is taken to have the form

$$f = f_0 + \xi \chi_x + \eta \chi_y, \quad (2)$$

where f_0 is the Fermi distribution function, and the functions χ_x and χ_y (found with the aid of the kinetic equation, in which the term taking into account collisions, was derived by Lorentz³) equal:

$$\chi_x = -l(f_1 - qf_2) / v(1 + q^2), \quad (3)$$

$$\chi_y = -l(f_1 q + f_2) / v(1 + q^2).$$

Here l is the length of the mean free path of the electron, and the rest of the variables are defined as follows:

$$q = \omega l / v = (eH / mc) l / v; \quad (4)$$

$$f_1 = \partial f_0 / \partial x - eE_x \partial f_0 / \partial \varepsilon;$$

$$f_2 = \partial f_0 / \partial y - eE_y \partial f_0 / \partial \varepsilon;$$

E_x and E_y are the components of the electric field resulting from the motion of the electrons under the action of the temperature gradient.

Calculation shows that the dependence of l on v for the present problem is immaterial, because the terms containing the derivative of l with respect

to v , are small and do not enter into the expression for the coefficient for thermal conductivity κ .

Making the usual calculation for the coefficient of thermal conductivity $\kappa = -Q_x / \partial T / \partial x$ (in the present problem $I_x = I_y = 0$, $Q_y = 0$) with accuracy to the terms $\sim (kT/\varepsilon)^3$ (ε is the Fermi level), we obtain

$$\kappa = \kappa_0 \left[1 - \frac{4\pi^2}{15} \left(\frac{kT}{mv^2} \right)^2 \frac{q^2(4 + 2q^2 + 3q^4)}{(1 + q^2)^3} \right], \quad (5)$$

where $\kappa_0 = \pi^2 n l k^2 T / 3mv$ is the coefficient of thermal conductivity in the absence of a magnetic field.

Approximate calculation shows that formula (5) gives a decrease in the thermal conductivity of less than 0.01% of κ_0 in a field of 10,000 Oersteds.

It can be shown that consideration of the effect is necessary for metals of the type of Bi which have a small number of conduction electrons.

In conclusion I must thank K. B. Tolpygo for a number of suggestions and E. I. Rashba for certain advice in the course of carrying out the work.

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Translated by F. P. Dickey
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Application of the Theory of Random Processes to Radiation Transfer Phenomena

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(Submitted to JETP editor April 17, 1956)

J. Exptl. Theoret. Phys. (U.S.S.R.) 31, 341-342

(August, 1956)

IN this note the motion of the photon is treated as a random process under the following very general assumptions: the medium is isotropic; its properties may be functions of time and space; the photon may be scattered, absorbed by an atom and reemitted, or absorbed in a collision of the second kind; the polarization of the radiation and the motion of the atom excited by a photon are not taken into account.

We begin with the function

$$f_{v_1}^{v_2}(\mathbf{r}_1, \eta_1, v_1, t_1; \mathbf{r}_2, \eta_2, v_2, t_2) dV_2 d\eta_2 dv_2,$$