

## Anisotropy of the Absorption of Gypsum Crystals in the Infrared Region

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A microscopic adapter and a polarizer were built for the infrared spectrometer, and the anisotropy of absorption and reflection of the gypsum crystals in the region  $2-11\mu$  investigated. For a series of spectrum bands corresponding to the vibrations of the molecules of water and  $\text{SO}_4$  groups, pleochroism and splitting into variously polarized components were observed. The origins of some bands were determined and conclusions were drawn about the character of coupling of vibrations in the lattice.

**1.** THE infrared spectra of gypsum crystals have been investigated several times since the end of the last century. The old investigations were reviewed by Shefer and Matossi<sup>1</sup>. Recently Ellis<sup>2</sup> and Louisfert<sup>3</sup> investigated the absorption spectra of gypsum crystals in the wavelength region  $0.9-2\mu$ . Miller and Wilkins<sup>4</sup> investigated, together with other inorganic substances, the emulsion of crystalline gypsum powder in an organic oil. Matsumura<sup>5</sup> studied the spectra of a single crystal of gypsum in the region around  $3\mu$ .

Also, the Raman spectra of gypsum crystals have been thoroughly investigated. A most thorough investigation of these spectra was made by Krishnan<sup>6</sup>. Investigations in polarized light were carried out by Cabannes and Aynard<sup>7</sup>. They also analyzed the results for vibrations in the  $3000\text{ cm}^{-1}$  region.

Gross and Valkov<sup>8</sup> investigated the Raman scattering of gypsum in the region up to  $200\text{ cm}^{-1}$ , and they ascribed the detected vibration frequencies to the hydrogen bond.

Stekhanov<sup>9</sup>, studying the Raman spectra

of gypsum in the region of  $3000\text{ cm}^{-1}$ , detected in the neighborhood of the fundamental lines  $3486$  and  $3408\text{ cm}^{-1}$  a number of associated lines at the distance up to  $200\text{ cm}^{-1}$ . These lines are ascribed to the intermolecular vibrations.

The purpose of our work was to investigate systematically the anisotropy of the infrared absorption of gypsum crystals in the region of fundamental frequencies.

**2.** A spectrometer with an auto-collimator provided with a  $\text{NaCl } 70^\circ$  prism was used in the investigation. The focal distance of the mirrors was  $600\text{ mm}$ , the prism height was  $70\text{ mm}$ , and the height of the slits up to  $30\text{ mm}$ . The radiation detector consisted of a thermo-couple with an electro-optical amplifier.<sup>10</sup> The polarizer was composed of three laminae of selenium, each about  $3\mu$  thick. The maximum obtainable polarization exceeds  $90\%$ . The polarization planes of the monochromator and the polarizer were parallel to each other. The rotation of the polarization plane with respect to the specimen was realized by the rotation of the latter.

The absorption spectra were obtained by using thin ( $10-60\mu$ ) sheets of the crystal with a well-defined orientation. The measurements were made by using a microscopic adapter with the spectrometer. The adapter consists of two identical mirror objectives with an aperture of  $0.45$ . The first objective projects a nine-time reduced image of Nernst's rod on the object. The object with the reduced image of Nernst's rod is then magnified nine times and projected by the second objective through the polarizer on the entrance slit of the spectrometer (Nernst's rod appears in its natural size).

<sup>1</sup> K. Shefer and F. Matossi, *Infrared spectra*, ONTI, 1935.

<sup>2</sup> J. W. Ellis, *Phys. Rev.* **38**, 693 (1931).

<sup>3</sup> J. Louisfert, *J. Phys. Radium* **8**, 22 (1947).

<sup>4</sup> F. A. Miller and H. Wilkins, *Anal. Chem.* **24**, 1253 (1952).

<sup>5</sup> On Matsumura, *Mem. Faculty Sci., Kyusyu Univ.* **1B**, 1-3 (1951); *Chem. Abst.* 4365 i (1952).

<sup>6</sup> R. S. Krishnan, *Proc. Ind. Acad. Sci.* **A22**, 274 (1945).

<sup>7</sup> J. Cabannes and R. Aynard, *J. Phys. Radium* **3**, 137 (1942).

<sup>8</sup> E. F. Gross and V. I. Valkov, *Dokl. Akad. Nauk SSSR* **68**, 473 (1949).

<sup>9</sup> Stekhanov, *Dokl. Akad. Nauk SSSR* **92**, 281 (1953).

<sup>10</sup> B. P. Kozyrev, *Uspehki Fiz. Nauk* **44**, 173 (1951).

The use of the micro-adapter was necessary because of the difficulties in preparation of thin sheets of gypsum crystals with various orientations having sufficiently large dimensions. For our measurements specimens of dimensions of  $0.2 \times 1.5$  mm were sufficient.

It is easy to show that, for a given sensitivity threshold of the radiation receiver (which determines the resolving power of the spectrometer), the minimum area of the specimen depends on the aperture of the micro-adapter. The aperture found in micro-objectives for infrared spectrometers is not greater than 0.8, even in objectives of lower image quality. Attempts to use specimens with smaller areas than that determined by the aperture of the micro-adapter and thus not filling completely the monochromator, resulted actually in a sharp reduction of the resolving power of the spectrometer.<sup>11</sup> It should be noticed that, because of its relatively large aperture, the use of the micro-adapter introduces some uncertainty in the results of the experiments. This fact, and also the difficulties in preparation of thin sheets of gypsum crystals having an orientation perpendicular to the principal cleavage plane (010), obliged us to perform a series of measurements by the method of reflection. The source of radiations - Nernst's rod - was projected on the polished surface of the specimen by means of a spherical mirror. By means of a second spherical mirror the image of the source and the surface of the specimen is projected through the polarizer on the entrance slit of the spectrometer. The aperture of the beam is not greater than 0.1; the angle of incidence is  $4^\circ$ . Under these conditions there is practically no influence of the oblique incidence on the results of the measurements. The polished surfaces had been obtained on a well-developed single gypsum crystal.

3. The gypsum crystal  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  belongs to the monoclinic system. The crystal has a laminated structure and the principal cleavage planes separate the layers of water molecules between which the double layers of  $\text{Ca}^{++}$  ions and of complex ions  $\text{SO}_4^-$  are enclosed.

The structure of an elementary cell of gypsum (Fig. 1) was established by Wooster.<sup>12</sup>

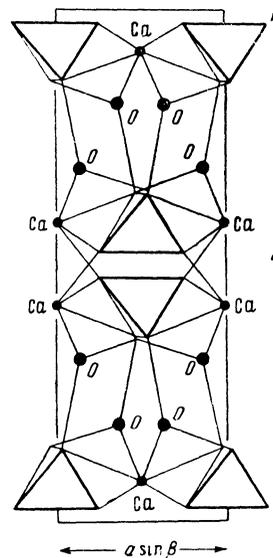


FIG. 1. The unit cell of gypsum according to Wooster. The tetrahedrons represent the  $\text{SO}_4^-$  groups. The positions of the hydrogen atoms of the water molecules are not shown.

Figure 2 (curve I) shows the absorption spectrum of a fine gypsum powder  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  as compared with the spectrum of  $\text{CaSO}_4 \cdot 0.5\text{H}_2\text{O}$  powder (curve II) and with the spectrum of anhydrous  $\text{CaSO}_4$  (curve III). It is known that the intense lines in the region  $1100-1200\text{ cm}^{-1}$  are related to the vibration of the  $\text{SO}_4^-$  ions. The  $1615\text{ cm}^{-1}$  line is obviously caused by deformational vibrations ( $\nu_2$ ) of the crystallization water molecules (in liquid water  $\nu_2 = 1640\text{ cm}^{-1}$ ). A weaker line,  $1675\text{ cm}^{-1}$ , could be observed in the spectra obtained by several investigators, beginning with Koblenz, but no suggestion was made to explain its origin. The  $2220\text{ cm}^{-1}$  line belongs to the crystallization water (Raman frequency); the  $2130\text{ cm}^{-1}$  line is due to the  $\text{SO}_4^-$  group (second harmonic of the  $1100-1200\text{ cm}^{-1}$  line). In the spectrum band  $3300-3600\text{ cm}^{-1}$  very strong absorption is observed. Certainly, here must appear the symmetrical  $\nu_3$ , and the anti-symmetrical  $\nu_2$ , vibrations of water molecules (in liquid water  $\nu_1 = 3450\text{ cm}^{-1}$ ;  $\nu_3 = 3580\text{ cm}^{-1}$ ). In the same region also should be situated the harmonics of the  $1675$ ,  $1615$ , and  $1100-1200\text{ cm}^{-1}$  lines. It is also possible that the  $3300-3600\text{ cm}^{-1}$  band is broadened by the presence of hydrogen bonds in the crystal.

<sup>11</sup> D. L. Wood, Rev. Sci. Instr. 21, 764 (1950).

<sup>12</sup> W. A. Wooster, Z. Kristall. 94, 375 (1936).

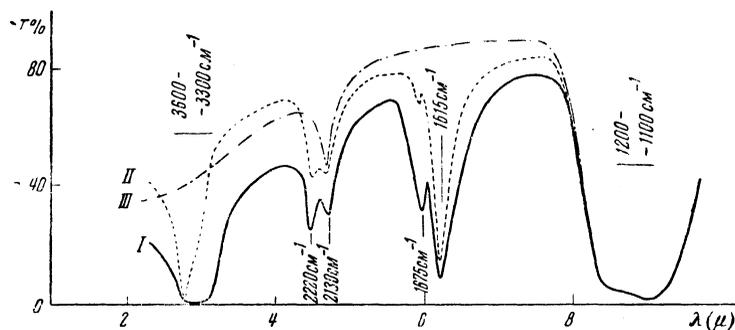


FIG. 2. The absorption spectra of gypsum powders  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  (curve I),  $\text{CaSO}_4 \cdot 0.5 \text{H}_2\text{O}$  (curve II) and  $\text{CaSO}_4$  obtained by heating to  $600^\circ \text{C}$  (curve III).  $T$  is the transmission coefficient of the specimens.

The absorption spectra of a lamina of gypsum  $50\mu$  thick, cut parallel to its principal cleavage plane, are represented in Fig. 3. The direction of the light beam coincides in this case with the  $b$  axis of the crystal. The electric vector was oriented either parallel to the direction of the fibrous cleavage of the crystal (curve II) or perpendicular to it (curve I). Curve III was obtained for a crystal cut parallel to the  $b$  axis and to the direction of the fibrous cleavage. The electric vector is in this case perpendicular to the  $b$  axis. The data obtained indicate a strong anisotropy of absorption of gypsum crystals. It was impossible

to obtain a full picture of the directions of maximum absorption for all lines; the attempts to resolve the  $3300\text{-}3600 \text{ cm}^{-1}$  band by using larger dispersion (LiF prism) and smaller thickness of the specimen (up to  $2\mu$ ) were unsuccessful. It was impossible also to resolve the band around  $1100\text{-}1200 \text{ cm}^{-1}$ . Therefore, an investigation was made of reflection spectra in polarized light. This enabled us to detect many important details. The results of these investigations are represented in Fig. 4. This figure shows also the directions of the incident radiation and of the vibrations of the electric vector.

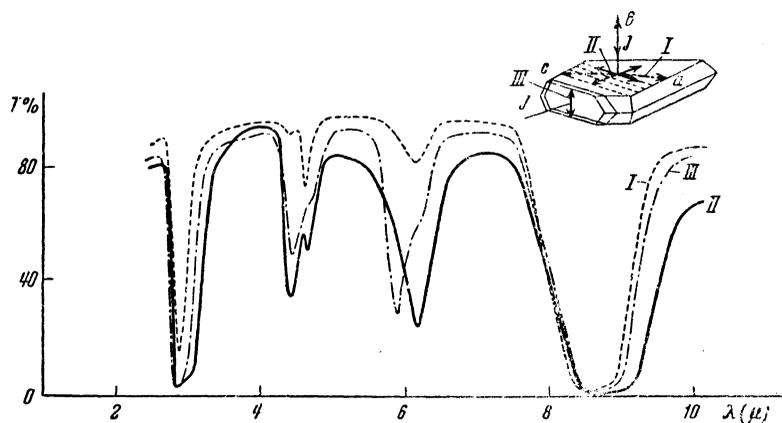


FIG. 3. The absorption spectra of gypsum crystal sheets in polarized light. The orientation of the cuts and the direction of the light polarization are shown in the figure.  $T$  is the transmission coefficient of the specimens.

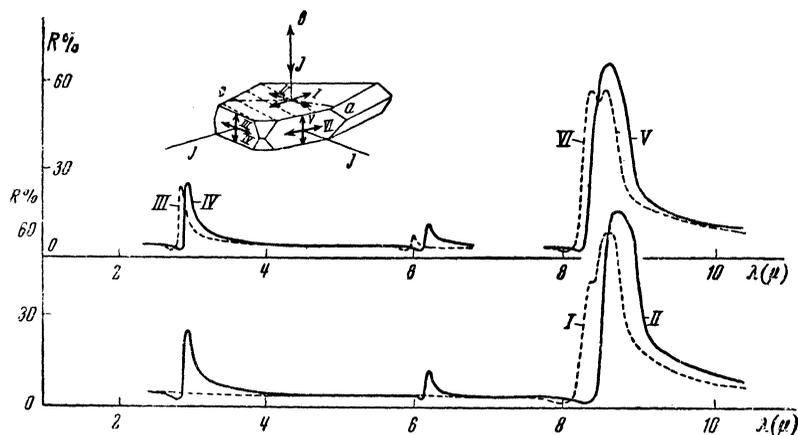


FIG. 4. The reflection spectra of gypsum crystals. The orientation of the polished surfaces and the direction of the polarization are shown in the figure.  $R$  is the reflection coefficient of the specimen.

The spectrum band  $1100\text{--}1200\text{cm}^{-1}$  shows a clear anisotropy in the reflection. On curves *I* and *VI* (Fig. 4) two components of this band are resolved. They are situated at about  $1180$  and  $1150\text{ cm}^{-1}$ . A third component appears on graphs *II* and *V*, but it was not possible to resolve it, even when a slit was used with a spectral width of  $3\text{ cm}^{-1}$  and the crystal cooled to the temperature of the liquid air. The maximum of this component is, according to our estimation, situated at about  $1120\text{ cm}^{-1}$ . It should be pointed out that dependence of the maximum on the orientation of the polarization plane is observed also in the second harmonic of the considered vibrations around  $2130\text{ cm}^{-1}$  (Fig. 3), but the influence of the neighboring  $2220\text{ cm}^{-1}$  line, associated with the crystallization water, makes the study difficult in this case.

The reflection spectra in the region  $1615\text{--}1675\text{ cm}^{-1}$  shown in Fig. 4 were obtained by taking into account the absorption due to the atmospheric humidity. Here also the dichroism clearly appears. The position of the observed lines, whose maxima are shifted by  $5\text{ cm}^{-1}$  in the direction of low frequencies with respect to the lines obtained by absorption, does not depend on the directions of observation and polarization. This is also true for the maxima of reflection in the region of valence vibrations of the water molecules which are situated around  $3400$  and  $3510\text{ cm}^{-1}$ . The second of these maxima is a little deformed because of the superposition of absorption lines of the atmospheric moisture. It is not clear, however, why

the broad band of absorption in the region  $3000\text{--}3600\text{ cm}^{-1}$  appears in the reflection spectrum only in the form of two narrow maxima and, moreover, why the line of absorption observed on curve *I* (Fig. 3) around  $3485\text{ cm}^{-1}$  does not appear in the reflection spectrum with corresponding orientation of the electric vector of the incidence radiation. These questions merit further study.

The results discussed above were obtained with an arbitrarily chosen orientation of the electric vector of the incidence radiation. In order to determine the direction of the maximum absorption, the polar diagrams of reflection were measured by rotating the investigated specimen around an axis perpendicular to the reflecting plane without changing the polarization plane. Analogous diagrams were also obtained by absorption. In this case, the spectrometer separated the narrow interval of wavelengths near the maximum of the investigated absorption band. The investigations were made on those specimens which had been used for the measurement of spectra. The obtained curves have a characteristic form of the figure eight. The direction of the greatest absorption coincides clearly with the long of the axis eight.

4. The directions of the absorption maxima were determined for the frequencies  $1120, 1150, 1180\text{ cm}^{-1}$  associated with the vibrations of atoms of the  $\text{SO}_4^{--}$  ion, and also for frequencies  $1615, 1675, 3400$  and  $3510\text{ cm}^{-1}$  associated with the vibrations of the molecules of crystallization water. The polar diagrams for the frequencies  $1120$  and  $1180\text{ cm}^{-1}$ , and particularly for the frequency  $1150\text{ cm}^{-1}$ , are a little

deformed, probably as a consequence of superposition of lines. Nevertheless, the asymmetry of the curves is very great, and the direction of the maximum absorption is defined without ambiguity.

The Table and Fig. 4 show the orientations of the dipoles for fundamental frequencies of vibrations, expressed by means of the angle of elevation  $\rho$  and the azimuth  $\varphi$  measured with respect to the axes  $b$  and  $a$  of the elementary cell of the crystal. The experimental values agree with the values computed on the basis of Wooster's model, according to which eight molecules of water present in the elementary cell of gypsum can be reduced, as a result of the crystal symmetry, to four identical orientations in space. If the dipoles responsible for the infrared absorption of water molecules in the crystal are orientated, as in free molecules, along the diagonal of the triangle H-O-H ( $\nu_1$  and  $\nu_2$ ) and along the normal to its plane ( $\nu_3$ ), then for each frequency the four dipoles would be grouped two by two in the directions shown on Fig. 5 and denoted by  $\nu_3$  and  $\nu_1, \nu_2$ .

The Directions of the Maximum Absorptions

Vibration Frequency in $\text{cm}^{-1}$	Values calculated on the basis of Wooster's model		Experimental Results	
	$\rho_0$	$\varphi_0$	$\rho$	$\varphi$
3510	40 140	33	0	—
3400	53 127	9	90	3
1675	—	—	0	—
1615	53 127	9	90	3
1180	90	100	90	103
1150	0	—	0	—
1120	90	10	90	25

The directions of the maximum absorption of the lines 1615 and 1675  $\text{cm}^{-1}$  coincide with the bisectrices of the angles between the vectors  $\nu_1$  and  $\nu_2$  Fig. (5).

Both these frequencies should be ascribed to the deformational vibrations of water molecules  $\nu_2$ ; the corresponding line, according to the theory of Davydov,<sup>13</sup> is separated into two mutually perpen-

dicular components. The ratio of intensities of these components is in qualitative agreement with the predictions of the theory. This interpretation agrees with the results obtained by comparison of the spectra of gypsum  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  with the spectra of  $\text{CaSO}_4 \cdot 0.5\text{H}_2\text{O}$  (Fig. 2). In this last case the line 1675  $\text{cm}^{-1}$  is not visible. The observed split of the line 1615-1675  $\text{cm}^{-1}$  indicates that deformational vibrations of individual water molecules in the gypsum crystal are not independent of each other and that the absorption and radiation in this special region is linked with the propagation of the excitation wave through the crystal.

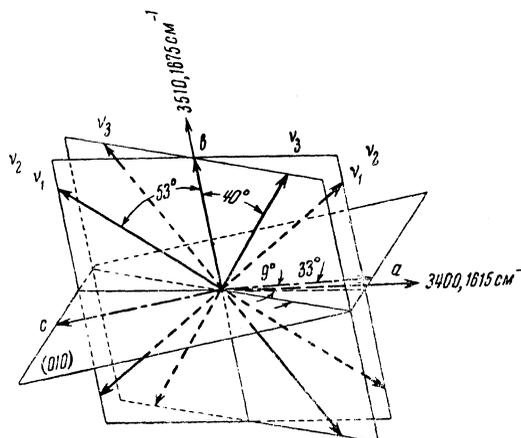


FIG. 5. The directions of the dipoles, corresponding to different vibrations of the water molecules, according to the model of the crystal, Fig. 1. The heavy arrows show the observed direction of the maximum absorption.

One would expect an analogous split of lines related to the valence vibrations of water molecules. In the corresponding region of the spectrum we found, however, the vibrations of two frequencies only: 3510  $\text{cm}^{-1}$  oriented (as 1675  $\text{cm}^{-1}$ ) along the  $b$  axis and 3400  $\text{cm}^{-1}$  oriented (as 1615  $\text{cm}^{-1}$ ) in the direction normal to the first one. The first of the frequencies should be related with the asymmetrical ( $\nu_3$ ) and the second with the symmetrical ( $\nu_1$ ), valence vibrations of the water molecules. We did not succeed, however, in detecting second components of these lines. One would conclude therefore from these results that the valence vibrations of individual water molecules in gypsum crystal are independent of each other, and that the excitation by light absorption has a localized character. It still re-

<sup>13</sup> A. S. Davydov, *Theory of Light Absorption in Molecular Crystals*, Trudy. Inst. Phys., Acad. Sci. USSR 1, 1951.

mains unexplained, however, why there is observed for each frequency a single, sharply defined direction of maximum absorption, coinciding with the bisectrix of the smaller angle between the corresponding dipoles (Fig. 5). Inasmuch as the angle between these dipoles is near  $90^\circ$ , with the direction of the incidence light normal to the planes  $\nu_1$  and  $\nu_3$ , the corresponding lines should exhibit only slight anisotropy. It has to be kept in mind that the data considered were obtained only by the reflection method and we see no reason to consider them as complete. It should be noted that Cabannes and Aynard<sup>7</sup>, studying the Raman spectrum of gypsum in polarized light, observed also in the same region only two components instead of the expected four. On the other hand, Matsumura<sup>5</sup>, whose paper we know only from a digest, discovered in the region of  $3\mu$  four components in the absorption spectrum of gypsum crystals. It is thus seen that the spectrum of valence vibrations of crystallization water in gypsum deserves further study.

Let us consider the spectrum of the group  $\text{SO}_4^{--}$ . As known, the vibrations  $1100\text{-}1200\text{ cm}^{-1}$  have a triple degeneracy. The field of the crystal splits them into three components, which in the slightly perturbed tetrahedron  $\text{SO}_4^{--}$  should be mutually perpendicular<sup>14</sup>. The orientations of the corresponding dipoles are the same for all  $\text{SO}_4^{--}$  groups; therefore, it cannot be expected that each of the components would be split.

The orientation of the component  $1120\text{ cm}^{-1}$  is not normal to the orientations of two other components (see Table). This deviation exceeds the limits of experimental error and is obviously caused by the asymmetry of the field of the crystal acting on the tetrahedron  $\text{SO}_4^{--}$ .

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<sup>14</sup> G. Herzberg, *Vibrational and Rotational Spectra of Polyatomic Molecules*.